

QFT Spring2025

HW5

Q1 Form Factors

Consider the classical electrostatic potential A^0 :

$$A^0(\vec{x}) = \int d^3y V(\vec{x} - \vec{y}) \rho(\vec{y})$$

where V is the Coulomb potential and ρ is the distribution of electric charges.

- a) Show that The Fourier transform of A^0 , $\tilde{A}^0(\vec{q})$ is given by the product of the Fourier transform of V and ρ , i.e.

$$\tilde{A}^0(\vec{q}) = \tilde{V}(\vec{q}) \tilde{\rho}(\vec{q}).$$

- b) Form factors are just $\tilde{\rho}(\vec{q})$.

For a point-like charge (Ze), $\tilde{\rho} = Ze$. (no q dependence). Compute analytic expressions of form factors for

- b1) Gaussian distribution

$$\rho(\vec{y}) = \rho_0 e^{-a^2 \vec{y}^2}.$$

- b2) Homogeneous sphere

$$\rho(r < R) = \frac{Ze}{4\pi R^3}$$

and zero otherwise.

Q2 Schwinger Dyson Equation for $\lambda\phi^4$ theory.

Derive the Schwinger Dyson Equation for the connected 2-point function. Identify the sunset diagram contribution.